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Methane adsorption and dissociation on iron oxide oxygen carriers: the role of oxygen vacancies

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We performed ab initio DFT+U calculations to explore the interaction between methane and iron oxide oxygen carriers for chemical looping reaction systems. The adsorption of CH_4 and CH_x (x = 0-3) radicals on α -Fe₂O₃(001), and the influence of oxygen vacancies at the top surface and on the subsurface on the adsorption properties of the radicals was investigated. The adsorption strength for CH_4 and Cradicals at the top of the α -Fe₂O₃(001) surface in the presence of oxygen vacancies is lower than that on the stoichiometric surface. However, for methyl (CH₃), methylene (CH₂) and methine (CH) radicals, it is correspondingly higher. In contrast, the oxygen vacancy formation on the subsurface not only increases the adsorption strength of CH_3 , CH_2 and CH radicals, but also facilitates C radical adsorption. We found that oxygen vacancies significantly affect the adsorption configuration of CH_x radicals, and determine the probability of finding an adsorbed species in the stoichiometric region and the defective region at the surface. With the obtained adsorption geometries and energetics of these species adsorbed on the surface, we extend the analysis to CH₄ dissociation under chemical looping reforming conditions. The distribution of adsorbed CH_4 and CH_y (x = 0-3) radicals is calculated and analyzed which reveals the relationship between adsorbed CH_x radical configuration and oxygen vacancies in iron oxide. Also, the oxygen vacancies can significantly facilitate CH₄ activation by lowering the dissociation barriers of CH₃, CH₂ and CH radicals. However, when the oxygen vacancy concentration reaches 2.67%, increasing the oxygen vacancy concentration cannot continue to lower the CH dissociation barrier. The study provides fundamental insights into the mechanism of CH₄ dissociation on iron based oxygen carriers and also provide guidance to design more efficient oxygen carriers

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1 Introduction

Chemical looping combustion (CLC) is a novel combustion technique in which metal oxide oxygen carriers are used as the oxygen source for heat generation.^{1,2} The CLC operation uses two reactors that are interconnected. One is a fuel reactor in which metal oxides are reduced by reacting them with the carbonaceous feedstock and the other one is an air reactor in which the reduced metal oxides from the fuel reactor are regenerated by re-oxidization with air. In the fuel reactor, CO2 generated from the oxidation reaction can be captured with 100% efficiency from the outlet of the reactor by simply condensing the steam, another reaction product, without engaging complex CO2 separation schemes. When biomass is used as the fuel, carbon emission in the life cycle assessment from chemical looping processes can be negative.3 This technology has been developed into a chemical looping partial oxidation (CLPO) process for direct syngas production from methane with significant economic attraction compared to the conventional approaches. In the CLPO process, oxygen carriers provide oxygen to partially oxidize methane in the fuel reactor or the reducer, thereby undergoing reduction themselves. The reduced oxygen carriers are then regenerated by air in the air reactor or the combustor and circulated back to the reducer. The oxidation reactions occurring in the combustor are highly exothermic and the heat generated can be used for power generation. The CLPO process can generate separate streams of high purity syngas from the reducer and an O2-depleted flue gas from the combustor, which obviates many downstream processing steps for the product generation, as illustrated in Fig. 1. This technique has been transformative and yields a highly efficient process of high economic benefits in the conversion of methane to syngas and hence a vast array of high value chemicals.4,5

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Air

Depleted air Syngas oxygen Oxygen CH₄ Adsorption carrier carrier carrier Dissociation oxidation reduction Oxygen carrier Reduced surface oxygen carrier

Fig. 1 The basic principles of CH_4 chemical looping reformation. CH_4 and CH_x radical adsorption and dissociation occur in the reduction section of the chemical looping system.

CH₄

Oxygen carriers play an important role in determining the product quality and process efficiency for the CLPO process. During reduction, the oxygen carrier donates the required amount of lattice oxygen for methane partial oxidation and form oxygen vacancies. In the oxidation step, the depleted oxygen carriers are replenished with oxygen from air while the oxygen vacancies are healed. Extensive research has been conducted in the design and development of efficient oxygen carriers. Oxygen carriers for successful chemical looping operation need to possess certain properties like high oxygen-carrying capacity, high fuel conversion, good redox reactivity, fast kinetics, good recyclability, long-term stability, high attrition resistance, good heat-carrying capacity, high melting point, resistance to toxicity, and low production cost. In addition, the applications for partial oxidation require certain distinct oxygen carrier properties to accurately control the product selectivity. Various oxygen carriers have been studied for CLPO applications, such as transition metal oxides of Co, Ni, Cu, Mn, W and Fe. 6-11 Among these oxygen carriers, iron oxide is very attractive since it is relatively inexpensive, readily available from large natural reserves and also environmentally safe. 12-14

Some studies of methane partial oxidation on iron oxide have been performed in recent years. Luo et al. 15 demonstrated that the Fe₂O₃-based oxygen carrier can generate syngas at a concentration higher than 90%, balanced by CO₂ and steam, with full fuel conversion. In their unique moving bed reactor configuration, the reactor is designed to operate with minimal carbon deposition and without the use of steam. The feedstock can be methane, biomass, coal, and other types of carbonaceous fuels, and H₂/CO may vary from 1:1 to 3:1 depending on the feedstock and operating conditions. Monazam et al.16 used thermogravimetric analysis to investigate the reduction of Fe₂O₃ in the methane atmosphere over the range of 700-825 °C with a continuous stream of CH₄ (15%, 20%, and 35%), and found that most of the CH₄ was totally oxidized into CO₂ and H₂O at the early stages of the reduction period, then CO and H2 were released due to partial oxidization of CH₄. Jin et al. 17 studied the reduction of Fe₂O₃ and evolution of gas products during CH₄ oxidation using TGA-MS under different reaction atmospheres, and reported that the ventilation air will hamper CH₄ oxidation.

As the key step of CH₄ oxidation, the C-H bond dissociation on metal surfaces has been intensively studied. Killelea et al. used state-resolved gas-surface scattering measurements which showed that the C-H stretch vibration selectively activates C-H bond cleavage on a Ni(111) surface. 18 Smith et al. reported that vibrational excitation of the antisymmetric C-H stretching activates methane dissociation more efficiently than translational energy.¹⁹ Yoder et al. presented a stereodynamics study of the chemisorption of vibrationally excited methane on the (100) surface of nickel, and found that the alignment of the vibrational transition dipole moment of methane is responsible for the steric effect.20 Krishnamohan et al. used quantum dynamics calculations to investigate the CH₄ reactivity on Ni(111) and concluded that the bending vibration greatly affects dissociation. 21 Nave and Jackson²² found that the Ni lattice reconstructs can effectively lower the C-H dissociation barrier based on first principles calculations, and also Tiwari et al.23 found that the thermal vibrations of the Ni lattice strongly modify the CH₄ reactivity. However, the interaction between iron oxides and methane has not still been fully understood due to the complex nature of Fe₂O₃ and limitations in experimentally detecting the dissociated CH_r radicals on the reaction surface using current spectroscopic techniques.

In addition, the relationships between oxygen carrier activity and its defective structure, especially oxygen vacancies, are not clear. As mentioned above, the oxygen carrier will donate lattice oxygen during methane partial oxidation which leads to the formation of oxygen vacancies. The vacancy sites act as initiators for the adsorption of molecules in many surface reactions. ^{24–28} It is therefore important to discern the stability of the different oxygen vacancies on the iron oxide surface, and their effect on the interaction between methane and oxygen carriers.

Ab initio DFT+U calculations can complement experimental mechanistic studies and provide valuable information on the structure of the active sites and the energy of the adsorbed species interacting with the surfaces. 29-31 In addition, detailed reaction pathways can be derived and characterized by the energy profile of the constituent elementary steps. 32 There have been a few DFT studies on the defect properties of Fe₂O₃. Warschkow et al. 33 built a slab model of the (001) surface of hematite as well as the bulk structure, and found that point defects are easier to form if they are closer to the top layer of surfaces, which is in agreement with our previous reported results.³⁴ Wanaguru et al.³⁵ modeled hematite nanoribbons, and showed that built-in oxygen vacancies can be produced on the edge. However, these studies only focus on the solid state and have not considered the relative surface reaction. Although the CH₄ dissociation mechanism for various materials has been widely studied, 36-39 there are few reports on the CH₄ dissociation mechanism on iron oxide. Wang et al.40 have used the density functional theory (DFT) method to investigate the interaction between CH₄ and Fe₂O₃ but they only used a Fe₂O₃ cluster model and did not include the oxygen vacancies in their system. No work has been reported on the effect of Fe2O3 vacancies on CH4 and CH_x radical adsorption and the corresponding CH₄ dissociation mechanism as far as we know. The lack of this knowledge will

hamper the design and development of oxygen carriers. Therefore, a detailed study of the role of oxygen vacancies in CH₄ adsorption and dissociation at the atomic level is highly desirable.

In this study, we present DFT+U and thermochemistry analysis of CH₄ and CH_x (x = 0–3) radical adsorption and dissociation on the stoichiometric α -Fe₂O₃(001) surface and the defective α -Fe₂O₃(001) surface with different oxygen vacancies. The study of adsorption and dissociation with vacancy defects will directly be of value to the future computational quantum mechanical and thermodynamic account of the partial oxidation pathways and to design more efficient oxygen carriers for the CLPO process.

2 Computational model and method

The first-principles calculations were performed within the framework of density functional theory (DFT), using the Vienna Ab Initio Simulation Package (VASP).41-43 The generalized gradient approximation of Perdew, Burke and Ernzerhof⁴⁴ was used to represent the exchange-correlation energy. The projector-augmented wave (PAW) method, 45,46 with a 400 eV energy cutoff, was used to describe the wave functions of the atomic cores. The tetrahedron method with Blöchl corrections⁴⁷ was used to set the partial occupancies for the orbitals. The calculated α -Fe₂O₃ bulk lattice parameters were a = b = 5.04 Åand c = 13.83 Å, in good agreement with the experimental values $(a = b = 5.038 \text{ Å and } c = 13.772 \text{ Å}).^{48} \text{ The } \alpha\text{-Fe}_2\text{O}_3(001) \text{ surface with}$ Fe-O₃-Fe-termination was chosen to model the iron oxide slab with a thickness of ~ 15 Å. We used (2×2) surface unit cells, and a vacuum region of 20 Å which ensures negligible interaction between periodic replicas. While several k-point mesh sizes (e.g., $4 \times 4 \times 1$ up to $13 \times 13 \times 1$) were considered, ultimately the 8 \times 8 \times 1 Monkhorst-Pack k-point mesh was used for surface calculations. Geometries were optimized until the energy had converged to 1.0×10^{-5} eV per atom and the force converged to 0.01 eV Å-1. The spin restricted method was used for the investigation of the oxygen vacancy formation on the α-Fe₂O₃(001) surface and spin-unrestricted calculations for the study of the CH_x radical (x = 0-3) adsorption on the stoichiometric and reduced α-Fe₂O₃(001), respectively. The on-site Coulomb repulsion amongst the localized 3d electrons is not described very well in a spin-polarized DFT treatment. To consider this Coulomb repulsion explicitly, we used DFT+U correction, which consists of combining DFT with a Hubbard-Hamiltonian term. 49,50 Increasing *U* from 1 eV to 4 eV results in improved values for magnetic moments and band gaps as well as better agreement with density of states by experimental IPS spectra. A further increase in *U* cannot achieve better agreement. In addition, the band gap becomes too large and occupied Fe 3d states are shifted to too low energies, i.e., U > 4.2 eV. Therefore, we choose U = 4 eV to describe the energy required for adding an extra d electron to the Fe atom.⁵¹

The oxygen vacancy formation energies are calculated based on the following expression:

$$E_{\rm f} = E_{\rm tot} = E_{\rm V} - \frac{1}{2} E_{\rm O_2}$$
 (1)

In eqn (1), E_{tot} is the total energy of the stoichiometric surface, E_{V} is the total energy of the reduced surface with one oxygen vacancy, and E_{O_2} is the total energy of the optimized gas phase O_2 . The adsorption energies of CH_x (x = 0–3) radicals on the stoichiometric and reduced surfaces are calculated using the expression as follows:

$$E_{\rm ad} = E_{\rm CH_{\perp}} + E_{\rm surf} - E_{\rm (CH_{\perp} + surf)} \tag{2}$$

where E_{CH_x} is the energy of the optimized gas phase geometry of CH_x , E_{surf} is the total energy of the respective surface, and $E_{(\mathrm{CH}_x+\mathrm{surf})}$ is the total energy of the slab with adsorbed CH_x . Based on this definition, a more positive E_{ad} corresponds to a more stable configuration.

The C atom of CH_x radicals may bond to lattice oxygen atoms on the surface. To analyze the bonding effect and strength, the bond order n of the C–O bond has been calculated as follows:

$$n = aR^{-2} - b \tag{3}$$

where *R* is the C–O bond length in Å. According to Gordy theory, we can set $a = 5.75 \text{ Å}^2$ and $b = 1.85.^{52}$

For CH₄ dissociation barrier calculations, the climbing-image nudged elastic band (CI-NEB) method was used.^{53,54} This method enabled the stationary points to be mapped out along the minimum energy paths and identify transition states for each of the diffusion processes. Because these paths were directed by force projection, the energy was not necessarily consistent with the force being optimized; thus, the force-based optimizer was chosen to ensure the convergence of the nudged elastic band algorithm.

3 Results and discussion

3.1 Oxygen vacancy formation

Iron oxide has been proved to be an efficient oxygen carrier for reduction–oxidation (redox) chemistry in $\mathrm{CH_4}$ chemical looping reformation, where it mediates $\mathrm{CH_4}$ oxidation through the release of oxygen. In this process, adsorbed $\mathrm{CH_x}$ radicals on the surface accept an oxygen atom from the iron oxide and the oxygen vacancy is created. The calculated formation energies for different surface and subsurface oxygen vacancy defects ($\mathrm{V_O}$) at the α -Fe₂O₃(001) surface are reported in Table 1. The labeling of the different vacancy sites is shown in Fig. 2.

By removing a 3-fold bridging oxygen (O3c), the vacancy on the top surface $V_O(1)$ can be created. It results in one 2-fold coordinated Fe (Fe2c) and two 5-fold coordinated Fe (Fe5c). This is found to be the energetically most favorable oxygen vacancy with the vacancy formation energy of 258.56 kJ mol⁻¹, while the vacancy formation energies for $V_O(2)$ and $V_O(2)$ are 292.51 kJ mol⁻¹ and 342.43 kJ mol⁻¹, respectively (Table 1). The Fe–O bonds of the neighboring Fe2c become symmetric with a bond length of 2.03 Å when the $V_O(1)$ oxygen vacancy is formed. The fact that the slight atom movement requires less energy and will not cause breaking of the neighboring bond makes $V_O(1)$ the most stable vacancy. The vacancy on the subsurface $V_O(2)$ can be created by removing a 4-fold bridging oxygen (O4c),

Table 1 Energy of formation for different oxygen vacancies in α -Fe₂O₃(001), the minimal and maximal length of Fe-O bonds around the vacancy (d_{min} and d_{max} , respectively), and the probability of $V_{\text{O}}(2)$ and $V_{\text{O}}(3)$ vacancies at 700 °C and 900 °C (relative to Vo(1))

	E_{f} (kJ mol ⁻¹)	$d_{\min} \choose { m (\AA)}$	$d_{ m max} \ m (\AA)$	Relative probability at 700 °C (%)	Relative probability at 900 °C (%)
V _O (1)	258.56	2.03	2.03	100	100
$V_{O}(2)$	292.51	1.93	2.09	1.51	3.07
$V_{O}(3)$	342.43	1.91	2.13	3.13×10^{-5}	1.84×10^{-4}

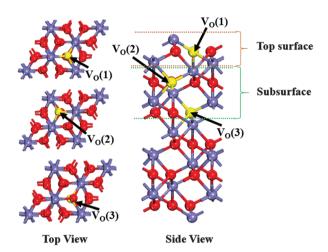


Fig. 2 α -Fe₂O₃(001) slab model with oxygen vacancies on the top surface and the subsurface (Fe = purple, O = red, oxygen vacancy = yellow).

and this process leads to asymmetric Fe-O bonds ranging from 1.93 Å to 2.09 Å. Similarly, the vacancy on the next subsurface $V_{O}(3)$ is also formed by removing a 4-fold bridging oxygen (O4c). However, V_O(3) formation energy is 83.87 kJ mol⁻¹ higher than $V_0(1)$ formation energy. Therefore, for α -Fe₂O₃(001), the oxygen vacancies on the top surface are more stable than the vacancies on the subsurface, which is different from anatase TiO2 in which the oxygen vacancies on the subsurface are more stable.⁵⁵

The presence probabilities of the different oxygen vacancies of α -Fe₂O₃(001) at 700 °C and 900 °C are also shown in Table 1. It is found that Vo(3) does not play a significant role in the adsorption of CH_4 and CH_x radicals (x = 0-3) due to high formation energy and low probability.

3.2 Adsorption of CH₄ and CH_x radicals on α-Fe₂O₃(001)

In this section, we discuss the adsorption of methane and the dissociated radical species on α-Fe₂O₃(001) as well as the influence of the different oxygen vacancies $(V_O(1))$ on the top surface and $V_0(2)$ in subsurface) on this adsorption. The different adsorption configurations are indicated as CH_x@S-y or $CH_x \otimes Vo(n)$ -y, where x (0-4) is the adsorbed species (CH_4 , CH₃, CH₂, CH and C), S denotes the stoichiometric surface, Vo(n) = defective surface with a $V_O(n)$ (n = 1, 2) oxygen vacancy, and y is an index used for identifying specific adsorption configurations. y consists of a letter from "A" to "D", where A denotes the surface iron atop site (on top of the Fe site on the surface layer), B denotes the surface oxygen atop site (on top of the O site on the surface layer), C denotes the Fe-O bridge site (between Fe and O on the surface layer) as shown in Fig. 3, D denotes the oxygen vacancy site, respectively. For example, CH@S-A corresponds to CH radicals (x = 1) adsorbed at the Fe atop site (y = A) on the stoichiometric surface; $CH_2(a)V_0(1)$ -D is CH_2 (x = 2) adsorbed at the oxygen vacancy site (y = D) on the reduced surface with a Vo(1) vacancy.

3.2.1 Adsorption on a stoichiometric α -Fe₂O₃(001) surface. We start by investigating the adsorption of CH₄ on the stoichiometric α-Fe₂O₃(001) surface so that we can obtain energy and structural information for the comparison of adsorption with vacancies. Various adsorption configurations on the stoichiometric α-Fe₂O₃(001) surface are modeled, optimized and calculated as reported in Table 2. For the considered configurations, the methane molecule shows weak interaction with the α-Fe₂O₃(001) surface. In the most favorable case, CH₄ adsorbs at the iron site as shown in Fig. 3(right), with an adsorption energy of 5.78 kJ mol⁻¹. The distance between the C atom and the Fe site in this case is 2.98 Å.

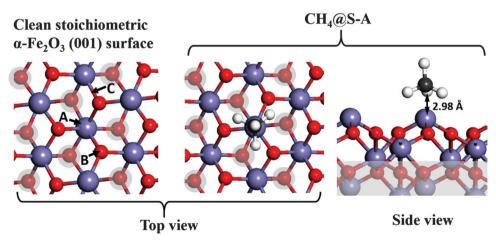


Fig. 3 Adsorption sites on the stoichiometric α -Fe₂O_x(001) surface and the most stable CH₄ adsorption configuration CH₄@S-A. The red ball with a gray circle in the top view and a gray area in the side view represent the oxygen atom on the subsurface and the subsurface layer, respectively. The distance between the C atom and the closest surface Fe atom is indicated

The O atop and Fe-O bridge adsorptions show lower stability with an adsorption energy of 2.81 kJ mol⁻¹ and 3.02 kJ mol⁻¹, respectively. All these energy values are very small, showing a weak interaction between CH4 and the stoichiometric α -Fe₂O₃(001) surface.

In order to obtain insights into the analysis of CH₄ dissociation on the α -Fe₂O₃(001) surface, we examine the adsorption of CH_x radicals. CH₃ is the first intermediate during CH₄ dissociation, and two stable adsorption configurations are found. In the most stable configuration, CH₃@S-A, the C atom in CH₃ is directly bonded to the surface iron site. In this case, the charge is transferred from the surface to the adsorbed CH3. This configuration has an adsorption energy of 31.57 kJ mol⁻¹. In the second stable configuration, CH₃@S-C, CH₃ is bonded to the Fe-O bridge site with the Fe-C bond of 2.75 Å and the C-O bond of 1.89 Å. CH₃@S-C is found to be 7.86 kJ mol⁻¹ less stable than CH₃@S-A. The formed C-O bond shows single bond character (C-O bond order $n = 0.97 \approx 1$). We also performed calculations on the adsorption of CH3 at the oxygen atop site, but this led to spontaneous desorption of CH₃ radicals.

For the adsorption of the CH_2 radical on the α -Fe₂O₃(001) surface, three stable adsorption configurations are found. CH2 adsorption at the iron atop site CH2@S-A is the most stable CH2 adsorption configuration with an adsorption energy of 121.33 kJ mol⁻¹. The second stable adsorption is CH₂ adsorption at the oxygen atop site CH₂@S-B, which shows the adsorption energy of 118.75 kJ mol⁻¹. The third stable configuration CH₂@S-C is about 30 kJ mol⁻¹ less stable than CH₂@S-A. For the CH radical, three different adsorption configurations are found. CH@S-A is the most stable configuration with 273.67 kJ mol⁻¹ adsorption energy. The difference with the second stable configuration CH@S-C is small: the adsorption energy is only 10.89 kJ mol⁻¹ higher for CH@S-A relative to CH@S-C. The oxygen atop site adsorption is relatively unstable with an adsorption energy of 183.23 kJ mol⁻¹. For a C radical adsorbed on the stoichiometric α-Fe₂O₃(001) surface, we find three different stable adsorption configurations, which in order of stability are indicated as CH@S-B, CH@S-A and CH@S-C. CH@S-B corresponds to the adsorption of C at the surface three-fold oxygen site O3c. Their adsorption energies are 533.98, 467.26 and 435.38 kJ mol^{-1} , respectively. The decrease in stability coincides with an increase in the Fe-C and C-O bond lengths, from 1.98 to 2.38 Å and 1.23 to 1.46 Å, respectively.

3.2.2 Adsorption on the defective α -Fe₂O₃(001) surface with oxygen vacancies. Understanding the effect of oxygen vacancies on the adsorption of species on the surface is essential for a more fundamental understanding of lattice oxygen vacancy

Table 2 Adsorption energies (in kJ mol⁻¹) of CH_4 and CH_x radicals on the stoichiometric α -Fe₂O₃(001) surface in different configurations

	CH_x radicals					
	CH_4	CH_3	CH_2	CH	С	
A. Fe atop	5.78	31.57	121.33	273.67	467.26	
B. O atop	2.81	_	113.75	183.23	513.38	
C. Fe-O bridge	3.02	23.71	90.24	262.78	435.38	

migration in oxygen carriers and their reaction activity. Here, we therefore study the influence of the two most stable vacancies $V_O(1)$ and $V_O(2)$ on the adsorption of CH_4 and CH_x radicals. We use D to denote the Vo(1) vacancy site when the oxygen vacancies are on the top surface, and also denote the Vo(2) vacancy if the oxygen vacancies are on the subsurface.

i. α -Fe₂O₃(001) surface with V_O(1) vacancy. First, we study CH₄ adsorption on the defective α-Fe₂O₃(001) surface. We found that the interaction becomes repulsive when V_O(1) vacancy is created. CH₄ still prefers to adsorb at the Fe atop site, but the neighboring oxygen vacancies make the adsorption energy of 2.87 kJ mol⁻¹ lower than the adsorption energy on the stoichiometric surface CH₄@S-A.

For adsorption of CH3, we previously found two stable adsorption configurations for the CH3 radical on the stoichiometric surface. However, four stable adsorption configurations are found on the reduced α -Fe₂O₃(001) surface with V_O(1) vacancy. The strongest adsorption is the CH₃ radical binding at the oxygen vacancy site to form CH₃@Vo(1)-D species with an adsorption energy of 202.65 kJ mol⁻¹, as shown in Fig. 4(a). The second and third stable configurations are CH3 adsorption at the Fe atop site CH₃@Vo(1)-A and CH₃ adsorption at the Fe-O bridge site CH₃@Vo(1)-C. The adsorption energies for these two configurations are 154.43 and 133.12 kJ mol⁻¹. We can see that the adsorption strength on the surface with $V_0(1)$ oxygen vacancy is higher than that on the stoichiometric surface. The presence of a V_O(1) vacancy thus stabilizes the adsorption of CH₃ on a Fe atom and Fe-O bridge site in the proximity of this vacancy. In addition, O atop adsorption configuration CH₃@Vo(1)-B is found to be stable on the reduced surface with an adsorption energy of 124.51 kJ mol⁻¹, which is unfavorable for CH₃ adsorption on the stoichiometric surface.

For adsorption of CH2, the adsorption interactions of CH₂@Vo(1)-A and CH₂@Vo(1)-D are found to be nearly identical with an adsorption energy of 317.42 and 309.14 kJ mol⁻¹, respectively. Their adsorption configurations with bond length are shown in Fig. 4(b) and (c). The difference between the most stable adsorption of CH2 on the stoichiometric surface and the adsorption of CH_2 on the reduced surface with a $V_0(1)$ vacancy is 196.09 kJ mol⁻¹. Again, the influence of $V_0(1)$ on the CH₂ radical adsorption is similar for CH3 radicals. The adsorption strength at both Fe atop and O atop sites shows a great increase with the presence of a V_O(1) vacancy. However, Fe-O bridge site adsorption becomes unstable for CH2 radicals. The charge distribution with $V_0(1)$ vacancy formation may cause the CH₂ radical at the Fe-O bridge site to move toward the Fe atop site or the O atop site.

For the adsorption of CH on the stoichiometric surface two stable adsorption configurations were previously found as shown in Fig. 4(d) and (e). Also, in this case, the adsorption interaction was found to be almost identical for CH@S-A and CH@S-C. However, this does not lead to the same result when a $V_0(1)$ vacancy is created. Similar to CH2 adsorption, the formation of vacancies makes Fe-O bridge adsorption unfavorable. However, the new adsorption configuration at the vacancy site

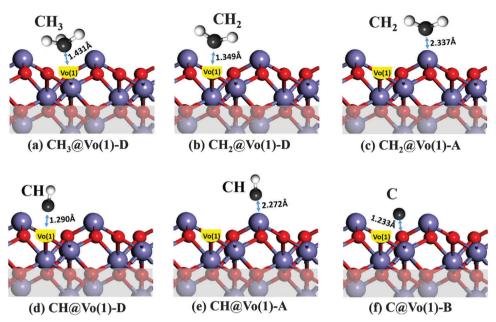


Fig. 4 The most stable CH_x radical adsorption configuration on the reduced α -Fe₂O₃(001) surface with V_O(1) vacancy. The distance between the C atom and the closest surface atom is indicated.

CH@Vo(1)-D shows approximately the same adsorption energy for CH (309.14 kJ mol⁻¹) as the adsorption of CH at the Fe atop site configuration CH@Vo(1)-A (317.42 kJ mol⁻¹).

Meanwhile, the Fe atop adsorption CH@Vo(1)-A becomes stronger than CH adsorption at the Fe atop site on the stoichiometric surface with 117.29 kJ mol⁻¹ higher adsorption energy. For the C-radical adsorption, we find four different stable adsorption configurations on the reduced surface with V_O(1) vacancy, which in order of stability are indicated as CH@Vo(1)-B, CH@Vo(1)-A, CH@Vo(1)-D and CH@Vo(1)-C. The corresponding adsorption energies are 489.62, 427.31, 410.65 and 392.83 kJ mol⁻¹. The strongest adsorption form a C-O bond of 1.223 Å as shown in Fig. 4(f). Compared with C radical adsorption on the stoichiometric surface, we found that the interaction between C and α -Fe₂O₃(001) becomes weaker when the Vo(1) vacancy exists at neighboring adsorption sites. By this detailed study of the effect of a $V_0(1)$ vacancy on CH₄ and CH_x radical adsorption, we found that for CH₃, CH₂ and CH radicals the interaction energy increases relative to the most stable adsorption on the stoichiometric surface. However, for CH₄ and C radicals, the adsorption energy dropped compared to the configurations on the stoichiometric surface. These results reveal the role of the Vo(1) vacancy in CH4 and CHx radical adsorption on the iron oxide surface which can provide fundamental insight into the CH_x radical evolution mechanism with the formation of lattice oxygen vacancies on the top surface.

ii. α -Fe₂O₃(001) surface with V_O(2) vacancy. Cheng et al. reported that the subsurface oxygen vacancies on the anatase TiO₂ surface are more stable than oxygen vacancies on the top surface.³² However, for the α -Fe₂O₃(001) surface, we have shown that the subsurface oxygen vacancy $V_0(2)$ is less stable than the top surface oxygen vacancy $V_0(1)$. At 900 °C, the relative probability of $V_0(2)$ is 3.07% thus its role in methane oxidation cannot be ignored.

For CH₄ adsorption on the defective α -Fe₂O₃(001) surface with V_O(2) vacancy, we found that the adsorption energy increases by 1.22 kJ mol⁻¹ compared to the adsorption on the α-Fe₂O₃(001) surface with V_O(1) vacancy and decreases by 1.65 kJ mol⁻¹ compared to the stoichiometric surface though the Fe atop site is still the most favorable site. In the presence of V_O(2) vacancy, the Fe atop site again becomes the most favorable site for CH3 radicals and the adsorption energy is 36.59 kJ mol⁻¹ higher than the adsorption energy at the $V_0(2)$ oxygen vacancy site. Apart from the adsorption configurations $CH_3@V_O(2)$ -A, $CH_3@V_O(2)$ -C and $CH_3@V_O(2)$ -D, which have similar adsorption structure and orientation to the corresponding adsorption on the α -Fe₂O₃(001) surface with V_O(1) vacancy, O atop configuration CH₃@V_O(2)-B is found to be unstable with a low adsorption energy (15.36 kJ mol⁻¹). This was close to the case for adsorption at the O atop site on the stoichiometric surface, where spontaneous desorption of CH_3 occurs. Also, from Tables 3 and 4 we can see that a $V_0(2)$ vacancy has a negative influence on the CH₃ adsorption strength compared to a $V_0(1)$ vacancy. Therefore, the migration of the $V_O(2)$ oxygen vacancy to a $V_O(1)$ vacancy can stabilize the adsorption of CH3 radicals on the iron oxide surface.

For adsorption of CH₂, it is found that the influence of the V_O(2) vacancy on CH₂@V_O(2)-A and CH₃@V_O(2)-D is almost identical, with an adsorption energy of 236.58 and 251.47 kJ mol⁻¹, respectively. The increase in the adsorption energy ranges from $\sim 70 \text{ kJ mol}^{-1} \text{ for } CH_2@V_O(2)\text{-C to } \sim 115 \text{ kJ mol}^{-1} \text{ for }$ $CH_2@V_O(2)$ -A relative to the adsorption on the stoichiometric surface. Compared to the stable CH3 adsorption on the α -Fe₂O₃(001) surface with V_O(1) vacancy, V_O(2) vacancy results in a drop in the adsorption strength, and the highest adsorption energy (CH₃@ $V_O(2)$ -D) drops by 57.67 kJ mol⁻¹. In this case, the Fe-C-Fe angle is 78.8°, compared to 62.7° for CH₃@V_O(1)-D,

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Table 3 Adsorption energies (in kJ mol^{-1}) of CH₄ and CH_x radicals on the reduced α -Fe₂O₃(001) surface with V_O(1) vacancy

	CH _x radicals				
	CH_4	CH_3	CH_2	CH	C
A. Fe atop B. O atop C. Fe–O bridge D. Vacancy	2.91 1.76 1.88	154.43 124.51 133.12 202.65	317.42 267.26 173.28 309.14	390.96 276.91 193.85 384.49	427.31 489.62 392.83 410.65

Table 4 Adsorption energies (in kJ mol⁻¹) of CH₄ and CH_x radicals on the defective α -Fe₂O₃(001) surface with V_O(2) vacancy

	CH_x radicals				
	$\mathrm{CH_4}$	CH_3	CH_2	CH	С
A. Fe atop	4.13	135.82	236.58	353.82	476.59
B. O atop	3.77	15.36	186.21	213.51	527.33
C. Fe-O bridge	2.10	129.23	166.29	272.32	469.27
D. Vacancy	2.13	89.11	251.47	344.22	489.61

and the two Fe-C bonds are elongated from 2.23 and 2.39 Å to 2.59 and 2.67 Å, respectively.

CH adsorption is found to be enhanced when V_O(2) is located below the C of the adsorbent, and the strength of adsorption is decreased when Vo(2) is located on the side of the O3c of the Fe-C-O-Fe structure. The presence of $V_0(2)$ leads to a shortening of the Fe-C bond in Fe atop adsorption configuration from 2.38 Å on the stoichiometric surface to 2.29 Å. The adsorption interactions of CH@Vo(2)-A and CH@Vo(2)-D are also nearly identical with an adsorption energy of 353.82 and 344.22 kJ mol⁻¹, respectively. Their adsorption configurations with the bond length are shown in Fig. 5(e) and (f). The difference between the most stable adsorption of CH radicals on the stoichiometric surface and

the adsorption of CH on the defective surface with a V_O(2) vacancy is $\sim 80 \text{ kJ mol}^{-1}$. The adsorption energy for O atop configuration CH@Vo(2)-B drops by 63.4 kJ mol^{-1} relative to CH@Vo(1)-B. While CH is adsorbed at the Fe-O bridge site in the CH@Vo(2)-C configuration, it is bonded to two O3c and the two Fe above the removed oxygen. It folds inward in the direction of the $V_0(2)$ vacancy, with a Fe-C-O angle of 65.3°. In this configuration, the O3c-C bond lengths are decreased from 1.42 Å (C-O bond order n=1) in CH@S-C to 1.37 Å (C-O bond order n=1.22). The Fe-O site adsorption energy also increases slightly relative to CH@S-C ($\Delta E_{\rm ad} \approx 10 \text{ kJ mol}^{-1}$). CH@Vo(2)-C on the other hand leads to surface relaxation, which causes the neighboring Fe-O bonds to elongate to ~ 2.15 Å.

For the adsorption of C radicals, the adsorption at the O atop site C@Vo(2)-B shows the highest adsorption energies (527.33 kJ mol⁻¹) while other three stable configurations: C@Vo(2)-A, C@Vo(2)-C and C@Vo(2)-D, give an adsorption energy of 476.59 kJ mol^{-1} , 469.27 kJ mol^{-1} and 489.61 kJ mol^{-1} , respectively. Compared to the adsorption on the stoichiometric surface, we can find that the subsurface oxygen vacancy slightly facilitates the C radical adsorption.

iii. α -Fe₂O₃(001) surface with a Vo(1) + V₀(2) vacancy. We extend our study to the α -Fe₂O₃(001) surface with a Vo(1) vacancy and a Vo(2) vacancy below the Vo(1) vacancy. Difference in the adsorption energy of the adsorption configurations on the defective α-Fe₂O₃(001) surface, relative to the adsorption on the stoichiometric surface, is summarized and plotted in Fig. 6. In Fig. 6(A), we can see that the oxygen vacancy formation slightly decreases the interaction between CH4 and the iron oxide surface, also the interaction between C radicals and the iron oxide surface. For CH3 radicals adsorption at the Fe atop site, the Vo(1) + Vo(2) co-effect can increase the adsorption

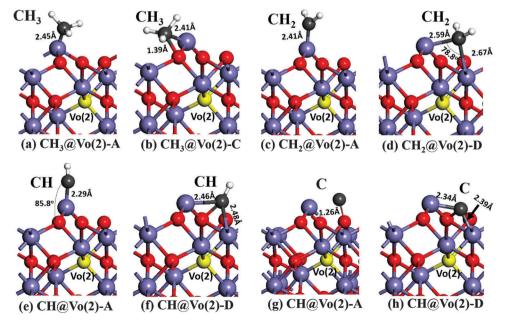


Fig. 5 The stable CH_x radicals adsorption configurations on the reduced α -Fe₂O₃(001) surface with $V_O(2)$ vacancy (yellow ball)

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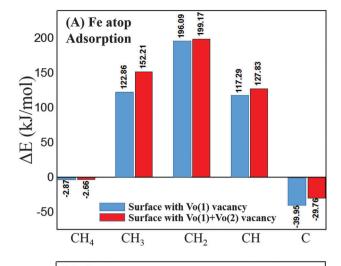
energy of 152.21 kJ mol $^{-1}$ compared to no vacancies, which is 23.8% stronger than the effect of Vo(1) vacancy. For CH $_2$ radicals, the adsorption with the Vo(1) + Vo(2) co-effect is only 2.1% stronger than the adsorption on the defective surface with one Vo(1) vacancy. However, the formation of the Vo(2) vacancy below the Vo(1) vacancy greatly increases the adsorption energy (\sim 200 kJ mol $^{-1}$) compared to adsorption on the stoichiometric surface. For CH radicals, the adsorption with the Vo(1) + Vo(2) co-effect is 8% stronger than the adsorption on the defective surface with one Vo(1) vacancy.

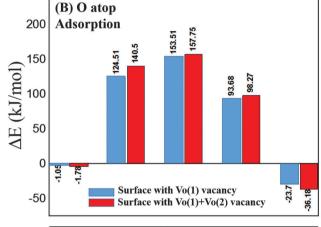
The difference between the adsorption energy of Fe-O bridge adsorption configurations of CH_x radicals on the α-Fe₂O₃(001) surface with a Vo(1) vacancy and that with Vo(1) + Vo(2) vacancies is shown in Fig. 6(C). We can see, for Fe-O bridge site adsorption, that Vo(2) vacancy formation exhibits a negative effect on CH₃, CH₂ and CH radical adsorption. The adsorption strength is 26.2%, 9.2% and 4.7% lower than the strength on the surface with only the Vo(1) vacancy. This is because the co-effect of surface relaxation due to the surface oxygen removal and the Fe-C-O complex formation due to CH radical adsorption shortens the Fe-O bond, which causes elongation of the formed C-O bond. In addition, compared to Fe atop adsorption and O atop adsorption, the Vo(1) + Vo(2) co-effect has a relatively weak effect on the Fe-O bridge adsorption of CH₃, CH₂ and CH. In the presence of the Vo(1) and Vo(2) vacancy, the adsorption energy of CH₃ binding at the Fe-O bridge site is 80.69 kJ mol⁻¹ higher than that on the stoichiometric surface, while it is 75.33 kJ mol⁻¹ higher for CH₂ radicals and 89.14 kJ mol⁻¹ higher for CH radicals. In contrast, the adsorption energy of CH3 binding at the O atop site of the surface with Vo(1) and Vo(2) vacancy is 140.5 kJ mol⁻¹ higher than that on the stoichiometric surface, and it is 157.75 kJ mol⁻¹ higher for CH₂ radicals. We also can see from Fig. 6 that the formation of the subsurface oxygen vacancies can further stabilize the adsorption of CH₃, CH₂ and CH radicals at the Fe atop site or the O atop site.

To investigate the Van der Waals interaction effect on adsorption on the stoichiometric and defective surfaces, we also calculated the dispersion energies using Grimme's DFT-D2⁵⁶ and found that the inclusion of this correction results in an increase in the adsorption energy by about 1–4 kJ mol $^{-1}$ eV for CH $_x$ species adsorption. For example, the adsorption energy for CH $_3$ @Vo(1)-D is 202.65 kJ mol $^{-1}$ without dispersion while it is 204.93 kJ mol $^{-1}$ with dispersion. Therefore, the Van der Waals interaction should not significantly affect the adsorption of CH $_x$ species is quite strong, and thus, dispersive forces play only a small role.

3.3 Effect of oxygen vacancies on the distribution of adsorbed CH_4 and CH_x (x = 0-3) radicals

We have shown that the presence of oxygen vacancies on the α -Fe₂O₃(001) surface can significantly influence the adsorption of CH₄ and CH_x (x = 0–3) radicals. Here we further analyze the probability of finding an adsorbed species either in a stoichiometric region of the surface or at or near an oxygen vacancy under equilibrium conditions. We divided the surface into two





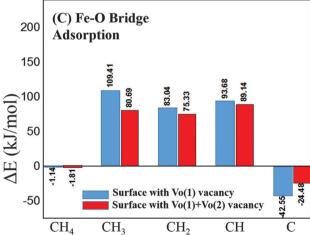


Fig. 6 Difference in the adsorption energy of the adsorption configurations of CH $_4$ and CH $_x$ radicals on the α -Fe $_2$ O $_3$ (001) surface with Vo(1) vacancy (blue bar) or Vo(1) + Vo(2) vacancy (red bar) relative to the adsorption on the stoichiometric surface.

regions: a stoichiometric region, where no oxygen vacancies exist near the adsorbed species, one region with $V_O(1)$ vacancy or $V_O(1) + V_O(2)$ vacancy. We use s to denote the stoichiometric surface, d for the defective region with $V_O(1)$ vacancy or $V_O(1) + V_O(2)$ vacancy.

Firstly, at temperature T, the average lifetime ρ_i of the adsorbed species i in the most stable configuration j can be calculated using the Frenkel equation:57

$$\rho_{i,j} = \frac{1}{v_{i,j}} \times \exp\left(\frac{E_{\text{ad},i,j}}{k_B T}\right) \tag{4}$$

where $v_{i,j}$ is the vibrational frequency of the adsorbed species i in the configuration j, $k_{\rm B}$ is the Boltzmann constant and $E_{{\rm ad},i,j}$ is the adsorption energy of the species i in adsorption configuration j. Then we can obtain the probability of finding the adsorbed species i in configuration j in the defective region dusing eqn (5):

$$P_{i} = \frac{\sum_{j}^{d} \left(n_{i,j} \times \rho_{i,j} \right)}{\sum_{j}^{s} \left(n_{i,j} \times \rho_{i,j} \right) + \sum_{j}^{d} \left(n_{i,j} \times \rho_{i,j} \right)}$$
(5)

where $n_{i,j}$ is the percentage of adsorption sites for the species iadsorption with configuration $j \cdot \sum_{i}^{s} \left(n_{i,j} \times \rho_{i,j} \right)$ which is the sum of the product of the average lifetime and the percentage of adsorption sites for the adsorbed species i with each stable configuration j in the stoichiometric region. The configuration jrefers to Fe atop, O atop and Fe-O bridge adsorption configuration; thus the sum is taken over three different configurations.

adsorption configuration besides Fe atop, O atop and Fe-O bridge adsorption configuration, thus the sum $\sum\limits_{i}^{d}\left(n_{i,j} imes
ho_{i,j}
ight)$ is taken

For the defective region, the configuration *j* also refers to vacancy

over four different configurations.

We give weights based on the vacancy equilibrium distribution on the defective surface at different temperatures. Obviously, $V_0(1)$ has a greater influence on the adsorption distribution because of a much higher abundance on the surface compared to $V_0(2)$. Also, $V_0(1)$ is easier to form than $V_0(2)$ due to lower vacancy formation energy as shown in Table 1. When the first oxygen vacancy Vo(1) is created, the vacancy concentration in the s + d region is 0.33%. The second, third and fourth vacancies also appear at the top surface. The distance between neighboring Vo(1) vacancies is about 5 Å. The fifth vacancy will form on the subsurface of the d region and the $V_0(2)$ vacancy formation energy is 39.5 kJ mol⁻¹ lower than that on the top surface. We have examined CH4 adsorption on the stoichiometric surface, the defective surface with a Vo(1) vacancy and with a Vo(2) vacancy, and found the most stable adsorption configurations with adsorption energies of 5.78 kJ mol⁻¹, 2.91 kJ mol⁻¹ and 4.13 kJ mol⁻¹, respectively. It cannot be accurate to calculate the probability of finding CH4 based on these small values due to the weak interaction with the surfaces. Therefore, we only investigate the probability of finding CH_x species. For CH_x radicals, at 900 °C, the calculated probability in the defective regions of the surface is shown in Fig. 7.

From Fig. 7, we can see the probability of finding the adsorbed CH_3 radical in the defective region d dramatically increases when oxygen vacancies are formed. It is 73% for

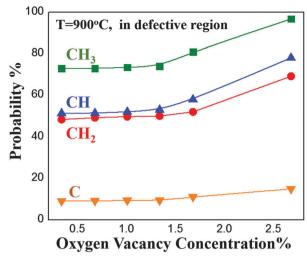


Fig. 7 Oxygen vacancy concentration dependence of the probability of finding an adsorbed CH_x radical in the defective region of the α -Fe₂O₃(001) surface.

0.33% vacancy concentration. On the other hand, the probability of finding the adsorbed CH3 radical in the stoichiometric region s greatly increases upon this vacancy formation. However, when the oxygen vacancy concentration is between 0.33% and 1.33%, the CH₃ radical probability in the defective region almost remains constant with the increase in the oxygen vacancy concentration. It is because the newly formed vacancy in the defective region has a very weak effect on the CH₃ radical adsorption due to the distance of ~ 5 Å. When the oxygen vacancy concentration further increases to 1.67%, which responds to the fifth oxygen vacancy formation on the subsurface, the CH₃ radical probability in the defective region reaches 81.3%. For a vacancy concentration of higher than 2.5%, we found that the CH₃ probability increases to 95%. This can be explained by the strong interaction between the CH3 radical and the oxygen vacancy site. Although the vacancy sites may not be enough for all CH₃ adsorption to form CH₃@Vo(1)-D configuration when the vacancy concentration is only 2.67%, the probability of 96.7% illustrates that CH₃ radicals prefer to be adsorbed onto Fe atop sites, O atop sites or Fe-O bridge sites which are close to vacancies, to form CH₃@Vo(1)-A, CH₃@Vo(1)-B or CH₃@Vo(1)-C configurations, rather than CH₃@S-A or CH₃@Vo(1)-C.

For the CH₂ radical, we found that the probability in the defective region is about 49.5% when the oxygen vacancy concentration is between 0.33 and 1.33%. It indicates that there is almost the same amount of adsorbed CH2 radicals in the stoichiometric region with the amount in the defective region when the vacancy concentration is very low. It agrees with the fact that CH₂ radicals show the preferential adsorption towards both Fe site and the oxygen vacancy site with almost the same adsorption energies. Similarly, for CH radicals, we found that the probability in the defective region is about 51% when the oxygen vacancy concentration is in the same range. When the oxygen vacancy concentration increases to 2.67%, the probabilities of adsorbed CH₂ and CH in the defective region increase up to 69.2% and 78.1%, respectively. In other words, when the vacancy concentration increases, the probability of

region.

finding the adsorbed $\mathrm{CH_2}$ and CH radicals in the stoichiometric region also decreases. However, from Fig. 7 we can see that there are still 30.8% $\mathrm{CH_2}$ and 21.9% CH radicals in the stoichiometric region even when the vacancy concentration is higher than 2.5%. This means that a fraction of $\mathrm{CH_2}$ and CH radicals obtained by $\mathrm{CH_3}$ dissociation can migrate to the Fe atop site in the non-defective region from vacancy sites where most $\mathrm{CH_3}$ radicals reside. Considering the adsorption stability, these adsorbed $\mathrm{CH_2}$ radicals will prefer to be in $\mathrm{CH_2@S-A}$ configuration in the stoichiometric region, and $\mathrm{CH@Vo(1)-D}$ configuration in the defective region. Likewise, we can conclude that the adsorbed CH radicals will prefer to be in $\mathrm{CH@S-A}$ configuration in the stoichiometric region,

and CH@Vo(1)-A and CH@Vo(1)-D configuration in the defective

From Fig. 7 we can see that the probability of finding the adsorbed C in the defective region is relatively low, compared to other CH_x radicals. It is about $\sim 9\%$ when the oxygen vacancy concentration is less than 2%. Different from the probability for CH_3 , CH_2 and CH radicals, the probability of finding the adsorbed C in the defective region will not significantly increase when the oxygen vacancy concentration is higher than 2.5%. It is only 14.3% when the oxygen vacancy is 2.67%. This can be explained by the fact that the formation of oxygen vacancy deceases the adsorption strength of C radicals. Thus, a large percentage of C radicals prefer to be adsorbed in the stoichiometric region, which can be called as C deposition leading to a decrease in the activity of the α -Fe₂O₃ surface.

The above-mentioned results clearly show that oxygen vacancies significantly influence the distribution of the adsorbed species at the surface and determine the adsorption configuration under equilibrium conditions. Increasing the oxygen vacancy concentration can cause higher probability of finding adsorbed CH_x (0–3) radicals in the defective region. Because of the strong interaction between CH_x radicals and oxygen vacancies, a higher oxygen vacancy concentration can lead to a stronger adsorption for CH_3 , CH_2 and CH_3 , or a weaker adsorption of C radicals, hence facilitating the surface reactions or reducing the C deposition. In addition, the probability analysis reveals the relation between structures and the adsorption position, also the possible migration paths of CH_3 radicals on the surface. These results are essential for understanding of CH_4 reaction on iron oxides.

3.4 CH₄ dissociation on defective α-Fe₂O₃ surfaces

We have investigated the adsorption of CH_4 and CH_x radicals on stoichiometric and defective $\alpha\text{-Fe}_2O_3(001)$ surfaces with oxygen vacancies. Based on the obtained adsorption configurations and adsorption energies, we can explore the CH_4 dissociation pathways and further reveal the role of oxygen vacancies of $\alpha\text{-Fe}_2O_3(001)$ surfaces.

In the oxygen carrier reduction section of the chemical looping system, adsorbed CH₄ will sequentially dissociate into CH₃, CH₂, CH and C radicals, and the corresponding pathway can be mapped using the CI-NEB method. However, we need to correct the dissociation barriers using a thermochemistry

model because the reaction temperature in the chemical looping system is usually higher than 700 $^{\circ}$ C.

We previously developed a modified Brønsted-Evans-Polanyi relationship to calculate the activation energy for the elementary steps of the metathesis reaction.⁵⁸ Here, we extend this method to calculate the activation energy for CH₄ dissociation under chemical looping conditions as follows:

$$E_{a}(T) = E_{a,DFT} + \alpha (\Delta H_{dis}(T) - \Delta E_{dis,DFT})$$
 (6)

where $E_{\rm a,DFT}$ corresponds to the forward activation energy barrier at 0 K, which is obtained from CI-NEB calculations. $\Delta H_{\rm dis}(T)$ is the dissociation enthalpy at finite temperature, which is calculated from the individual enthalpies of the initial state and the final state for the constituent elementary reactions. $\Delta E_{\rm dis,DFT}$ is the difference between the energies of the final state and the initial state at 0 K. The variable α denotes the relative position of the transition state compared to the initial (*i.e.*, $\alpha=0$) or final (*i.e.*, $\alpha=1$) state of the relevant elementary dissociation reaction. It can be obtained by considering which image in the CI-NEB calculations corresponds to the transition state. When the value of α is close to 0, it describes an initial-like transition state; thus, the activation energy may be kept at the DFT value. When the value of α is close to 1, it corresponds a final-like transition state and the activation energy is corrected using eqn (6).

To obtain enthalpy, H, estimates at finite temperature, T, for all adsorbed species and products, we correct the electronic energy for the zero point energy (ZPE) contribution and temperature variation using C_p :

$$H(T) = H(0 \text{ K}) + \int_{0}^{T} C_{p}(T') dT'$$
 (7)

Numerically, T=0 K results in an undefined value during the evaluation of $C_{\rm p}$, as the temperature appears in the denominator. We can approximate $H(0 \text{ K}) \approx H(1 \text{ K})$, and obtain its value by H(1 K) = U(0 K) + ZPE, where U is the total energy. The heat capacity $C_{\rm p} = T\left(\frac{\partial S}{\partial T}\right)_{\rm p}$ can also be computed numerically by differentiating $C_{\rm p} = T\left(\frac{\partial S}{\partial T}\right)_{\rm p}$

tiating the entropy. The vibrational entropy, S_{vib} , can be directly obtained from the vibrational partition function using the DFT-calculated frequencies.

Because the H atom will be produced in CH_4 dissociation, we examined H adsorption and found that they have equal adsorption energies of about 263 kJ mol^{-1} at the Fe atop site of the stoichiometric surface and the defective surface. However, for the oxygen atop site, the adsorption energies of H are 218 kJ mol^{-1} on the stoichiometric surface, and 247 kJ mol^{-1} on the defective surface, respectively. Based on the adsorption of CH_4 and the co-adsorption of CH_3 and H, the first step of CH_4 dissociation is examined and the reaction energy profile is mapped out, as shown in Fig. 8. T_81 denotes the transition state of CH_4 dissociation into CH_3 and H occurring on the stoichiometric surface while T_d1 denotes the transition state of CH_4 dissociation which proceeds on the defective surface. On the stoichiometric α -Fe₂O₃(001) surface, CH_4 dissociates on top of a Fe atom into CH_3 and H via the transition state T_81 .

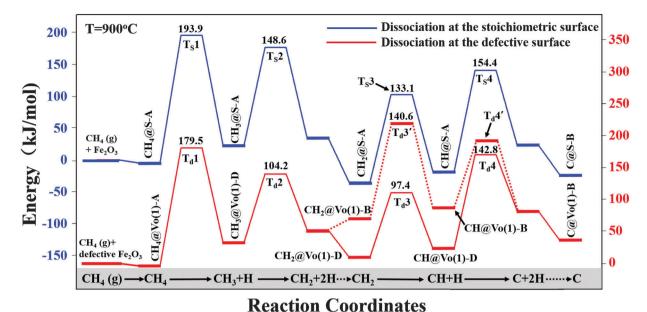


Fig. 8 Energy profile for CH₄ sequential dissociation on the stoichiometric and defective α -Fe₂O₃(001) surface ($T = 900 \, ^{\circ}$ C). T_S denotes the transition state on the stoichiometric α -Fe₂O₃(001) surface and T_d denotes the transition state on the defective surface.

The reaction needs to overcome the energy barrier of 193.9 kJ mol⁻¹. In the transition state T_s1, the breaking C-H bond is elongated to 1.611 Å, and the forming H-O bond is 1.361 Å. This reaction is endothermic by 27.3 kJ mol⁻¹. On the defective α-Fe₂O₃(001) surface, CH₄ dissociates via T_d1 along with CH₃ moving to the oxygen vacancy site while H remaining at the Fe atop site, and the corresponding barrier is 14.4 kJ mol⁻¹ lower than that on the stoichiometric surface.

Considering the most stable CH₃ adsorption configuration CH₃@S-A on a stoichiometric surface as the initial state and co-adsorbed configuration of CH2 and H as the final state, the transition state T_s2 of CH₃ dissociation is searched. We found that CH3 dissociates into CH2 and H along with H moving to another oxygen atop site which is opposite to the previous H obtained during the first step of CH₄ dissociation. The energy barrier is 148.6 kJ mol⁻¹, and it is kinetically favorable compared with the first dissociation step. For the dissociation of CH3 via T_d2 on the defective surface with Vo(1) vacancy, the calculated barrier is 104.2 kJ mol⁻¹, which indicates that oxygen vacancies can greatly affect the second step of CH4 dissociation. In the transition state T_d2, the distance of the breaking C-H bond is stretched to 1.685 Å, and the forming bond length of H-Fe is shortened to 1.396 Å nm. This reaction is found to be endothermic by 28.95 kJ mol⁻¹. On a defective surface with the top surface vacancy, the CH2 radical shows preferential adsorption towards both the Fe atop site and the oxygen vacancy site, thus two reaction pathways are conceived for CH₂ dissociation on the α-Fe₂O₃(001) surface with Vo(1) vacancy. In the transition state T_d3, the breaking C-H bond is increased to 1.741 Å, and the forming H-Fe bond is shortened to 1.372 Å. This dissociation via T_d 3 is also endothermic by 12.54 kJ mol⁻¹ and needs to overcome a barrier of 97.4 kJ mol⁻¹. If the initial state is $CH_2@Vo(1)$ -B, the dissociation needs to overcome a barrier of 140.6 kJ mol⁻¹,

which is approximately equal to the barrier of CH₂ dissociation on the stoichiometric surface (133.1 kJ mol⁻¹).

The last step of CH₄ full dissociation is the dehydrogenation of the methine radical CH to produce the C radical. We have found the C radical prefers to adsorb to O atop site both in the stoichiometric surface and the defective surface with oxygen vacancies. Co-adsorption of C and H atom has slight repulsive interaction compared with the sum of individual adsorption energies. On the stoichiometric surface, CH adsorption on Fe atop site is the most favorable configuration (CH@S-A). Based on these stable final states and initial states, we search for the local minimum on the potential energy surface and obtain a dissociation barrier of 154.4 kJ mol⁻¹ (T_S4). In contrast, the most favorable configurations for CH on the defective surface with oxygen vacancies are CH@Vo(1)-A and CH@Vo(1)-D. Thus, we consider two possible reaction pathways for the dissociation of CH on the defective surface: (1) the H atom remains at the Fe atop site and the C atom diffuses from the Fe atop site to the O atop site; (2) the H atom binds to the neighboring O atop site and the C atom diffuses from the oxygen vacancy site to the O atop site. The calculated dissociation barriers for (1) and (2) pathways are $146.33 \text{ kJ mol}^{-1}$ and $142.8 \text{ kJ mol}^{-1}$ (T_d4), respectively. If the initial state is CH@Vo(1)-B, the reaction barrier is even 21.3 kJ mol⁻¹ lower than the barrier of the second pathway where CH@Vo(1)-D is the initial state because no diffusion energy is required for this process. However, the O atop site is not favorable for CH adsorption, and the formation of CH@Vo(1)-B from CH2@Vo(1)-D must overcome a barrier of 156.9 kJ mol⁻¹ which is 46.8 kJ mol⁻¹ higher than the barrier of the most favorable CH2 dissociation pathway, as shown as the red dashed line in Fig. 8. Therefore, the dissociation pathway via CH@Vo(1)-B configuration is unfavorable. To analyze the whole energy profile along the dissociation paths, we found the

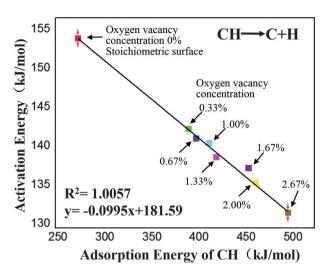


Fig. 9 Relationship between activation energy of the CH radical dissociation and adsorption energy of the CH radical. Oxygen vacancy concentration is labeled.

highest barrier is 193.9 kJ mol^{-1} for the dissociation on the stoichiometric surface, and 179.5 kJ mol^{-1} for the dissociation on the defective surface, respectively. They both are within the range of the reported experimental values (150–270 kJ mol^{-1}).⁵⁹

Since we have found that oxygen vacancies can facilitate the CH radical adsorption, we can further analyze the vacancy effect on the CH dissociation. Fig. 9 presents a good ($R^2 = 1.0057$) linear relationship between dissociation activation energy and the adsorption energy of the CH radical which is related to the vacancy position and concentration. We can see that the activation energy decreases with the increase of the adsorption energy of the CH radical on α-Fe₂O₃(001) surfaces. In other words, weaker adsorption brings higher activation energy. It is in agreement with the fact that low adsorption energy of CHx configurations is at high energy levels and thus they have to overcome a high activation energy barrier to dissociate. However, when the oxygen vacancy concentration is higher than 2.67%, increasing the oxygen vacancy concentration cannot continue to lower the CH dissociation barrier. Similar results are obtained for CH3 and CH₂ dissociation. On the other hand, too high oxygen vacancy concentration will decrease the oxygen carrier capacity of donating lattice oxygen for partial oxidation of CH4. Therefore, finding a suitable oxygen vacancy concentration is of great significance, which can lower the CH₄ dissociation barriers meanwhile can provide enough lattice oxygen for CH₄ partial oxidation. We have previously found that an inert support TiO2 can lower the vacancy formation energy thus can lead to the formation of oxygen vacancies.³⁴ Therefore, we can control the oxygen vacancy concentration of oxygen carriers to increase the activity of oxygen carriers by adding suitable support materials, which will be our future work.

4 Conclusion

Ab initio DFT+U calculations of methane and CH_x (0–3) radical adsorption on iron oxide was carried out to elucidate the geometries and energies of adsorption configurations on

stoichiometric and defective α-Fe₂O₃(001) surfaces with oxygen vacancies. We found that top surface oxygen vacancies are the most stable vacancies, compared to oxygen vacancies on a subsurface and the next subsurface. In the presence of these vacancies, the adsorption strength of CH4 and C radicals on the α -Fe₂O₃(001) surface decreases compared to that in the absence of vacancies, but it increases for methyl (CH₃), methylene (CH₂) and methine (CH) radicals. In contrast, the subsurface oxygen vacancy formation not only increases the adsorption strength of CH3, CH2 and CH radicals, but also facilitates C radical adsorption. However, oxygen vacancies on the subsurface have a smaller effect on CH_x radical adsorption compared to the top surface vacancies. The formation of the subsurface oxygen vacancies can stabilize the adsorption of CH3, CH2 and CH radicals. Specifically, the Fe atop site is the most favorable adsorption site for CH4 molecules. However, for the CH3 radical, the oxygen vacancy site is the most favorable adsorption site. The CH2 and CH radicals show preferential adsorption towards both the Fe atop site and the oxygen vacancy site, while the C radical prefers the O atop site on a defective surface.

The oxygen vacancies not only influence the adsorption strengths of $\mathrm{CH_4}$ and $\mathrm{CH_x}$ radicals on iron oxide, but also determine the distribution of $\mathrm{CH_4}$ and these corresponding radicals on the surface under equilibrium conditions. When the oxygen vacancy concentration is very low, increasing the oxygen vacancy concentration cannot cause higher probability of finding adsorbed $\mathrm{CH_x}$ radicals in the defective region. When the oxygen vacancy concentration is more than 2.5%, the probability of finding adsorbed $\mathrm{CH_3}$, $\mathrm{CH_2}$ and CH radicals in the defective region will evidently increase with the increase in the oxygen vacancy concentration. A higher oxygen vacancy concentration can lead to a stronger adsorption for $\mathrm{CH_3}$, $\mathrm{CH_2}$ and CH hence facilitating the surface reactions, or a weaker adsorption of C radicals, thus reducing C deposition. The probability analysis reveals the relation between structures and the adsorption position, also the possible migration paths of $\mathrm{CH_x}$ radicals on the surface.

In addition, oxygen vacancies can facilitate the $\mathrm{CH_4}$ dissociation on the iron oxide surface by lowering the dissociation barriers of $\mathrm{CH_3}$, $\mathrm{CH_2}$ and CH radicals. We found a linear relationship between the dissociation activation energy and the CH radical adsorption energy, which is determined by oxygen vacancy concentration. When the oxygen vacancy concentration is higher than 2.67%, increasing the oxygen vacancy concentration cannot continue to lower the CH dissociation barrier. Based on these results, future computational quantum mechanical and thermodynamic studies aiming to understanding methane partial oxidation can be envisaged. This study reveals the influence of oxygen vacancies on the $\mathrm{CH_4}$ and $\mathrm{CH_x}$ radical adsorption on iron oxide, and provides fundamental insights into the role of oxygen vacancies in the mechanism of $\mathrm{CH_4}$ dissociation for more active oxygen carrier design.

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